

# Towards a Cost-Effective Operation of Low-Inertia Power Systems

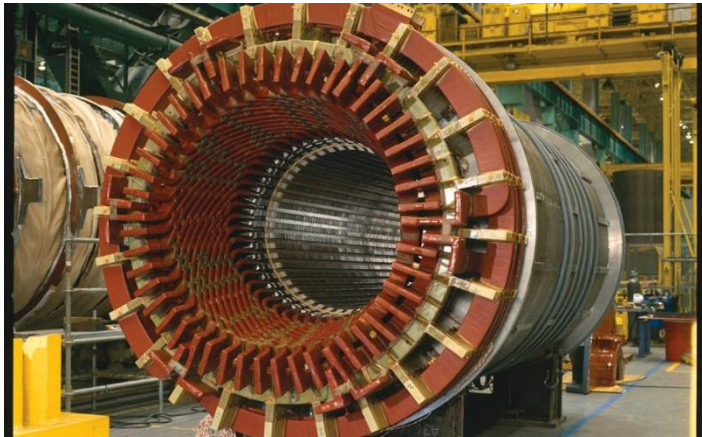
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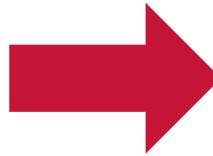
# Motivation: lower inertia on the road to lower emissions

“Inertia” means physical inertia, a **rotating mass**

*Thermal generators  
(nuclear, gas, coal...):*



*Most renewables:  
no inertia*

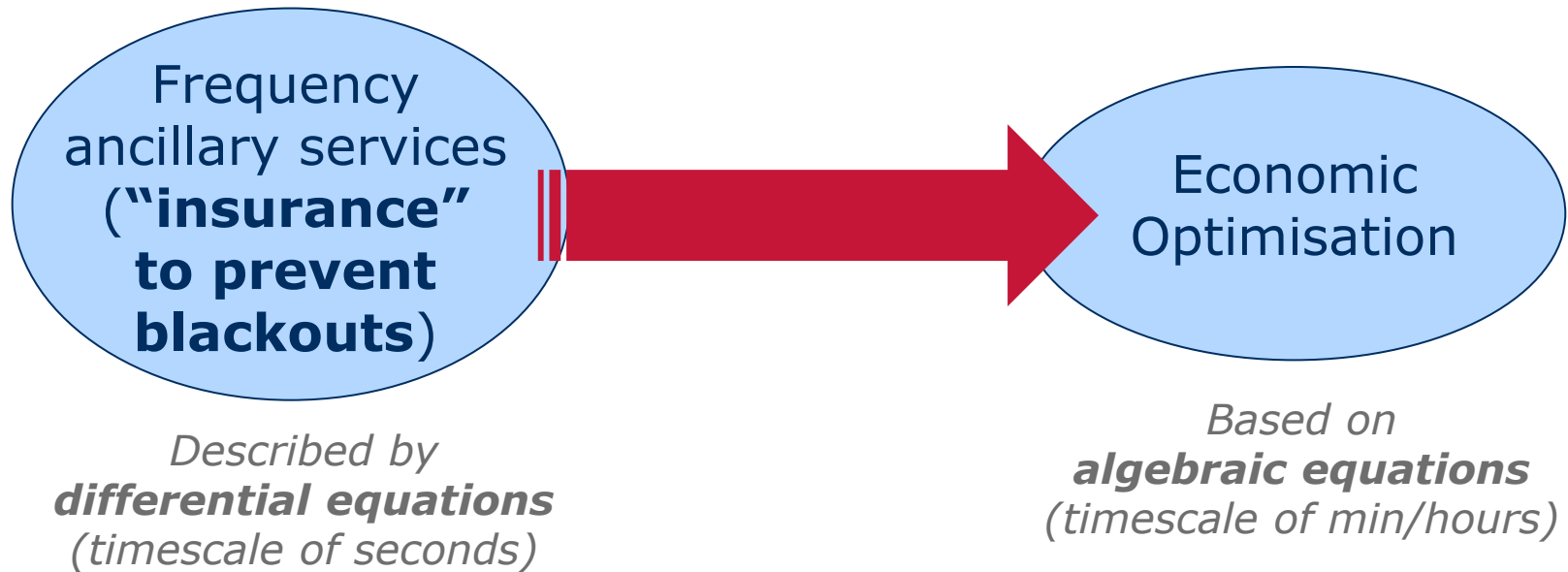


**Inertia stores kinetic energy:**  
this energy gave us time to contain a  
sudden generation-demand imbalance

**But now the risk of instability has increased** (e.g. [Great Britain blackout Aug 2019](#))

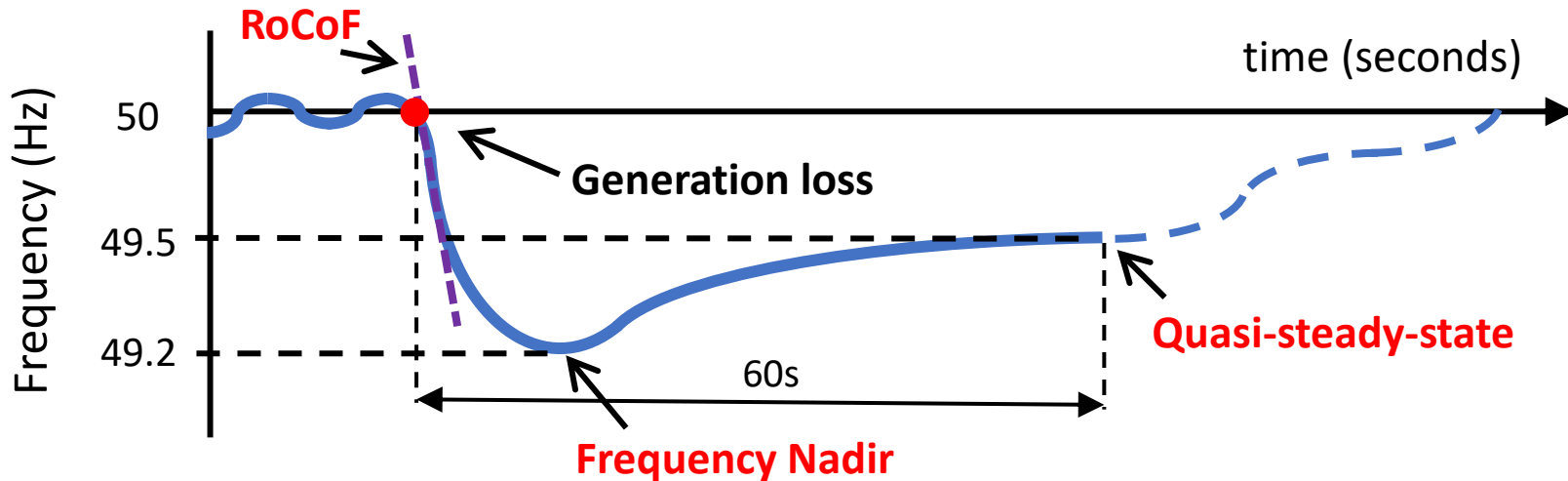
## My research question

*How to optimally procure the ancillary services needed because of low inertia?*



**Goal:** Achieve **minimum cost** while keeping the **system stable**

# Why is frequency important?



After a generation outage, the electric frequency of the grid drops.

**Devices can be damaged** if frequency falls too low: protection mechanisms disconnect generators and loads if they detect low frequencies.

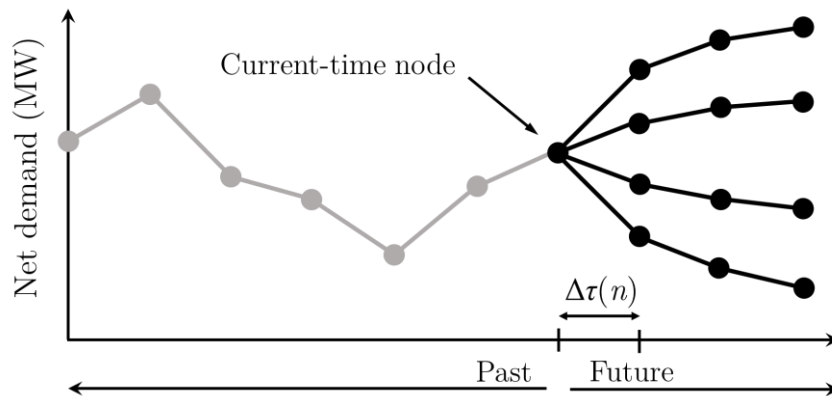
These disconnections, although necessary, **could lead to an eventual blackout.**

**Key to keep frequency within safe limits to avoid demand disconnection!**

# Scheduling and markets for energy and ancillary services

Analysis conducted with our **frequency-secured Stochastic Unit Commitment** model

1. Considers uncertainty from RES generation
2. Guarantees frequency stability

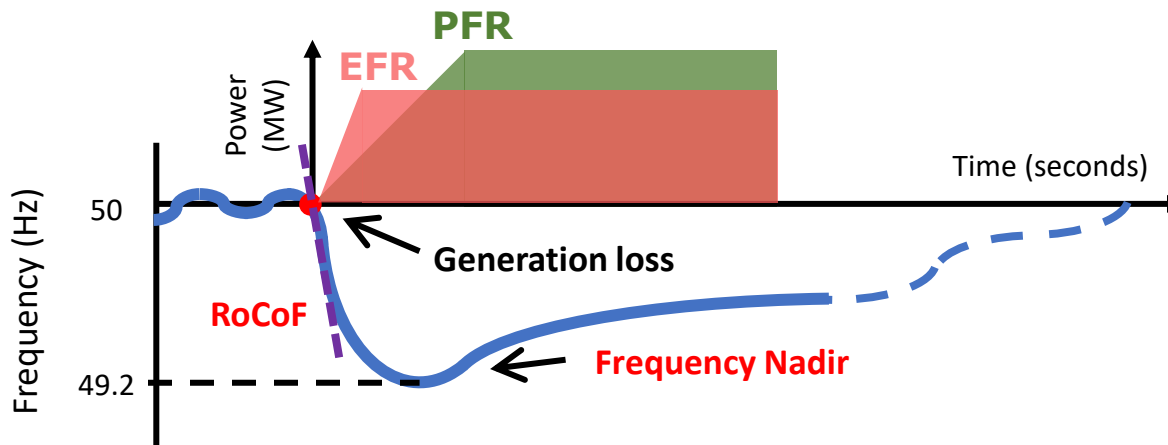


*Operating costs:  
fuel costs,  
start-ups, etc.*

$$\min \sum_{n \in \mathcal{N}} \pi(n) \sum_{g \in \mathcal{G}} C_g(n)$$

subject to  
RoCoF constraint  
Nadir constraint  
SteadyState constraint

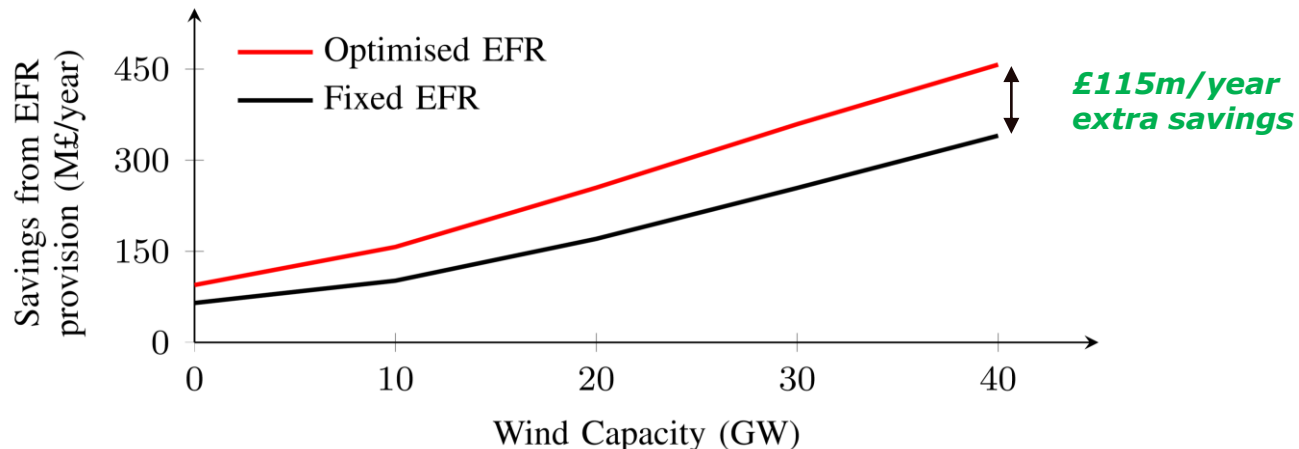
*(and other typical constraints)*



# Co-optimisation of multiple frequency services

Our models demonstrate the importance of co-optimising inertia and frequency response procurement. For example, **Enhanced Frequency Response (EFR) is not always needed**: it only becomes significantly more valuable than PFR when inertia is low

Instead of procuring a fixed-amount of 200MW of EFR at all times (current approach in GB), **co-optimising EFR procurement** can achieve **savings of up to £115m/year**



More info [here](#)

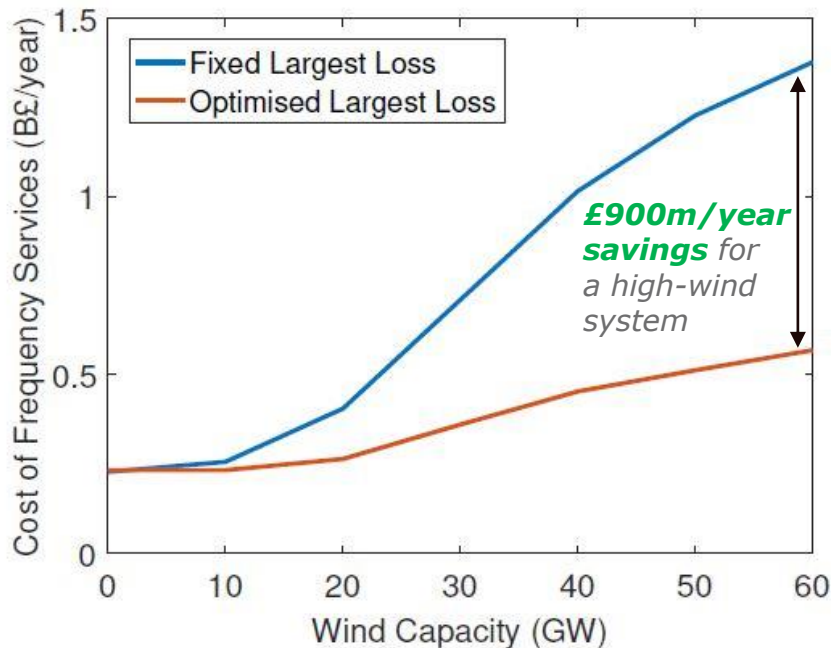
# Part-loading large nuclear to reduce the largest loss

Reducing the power output of large nuclear units **when it is optimal because it reduces the need for ancillary services:**

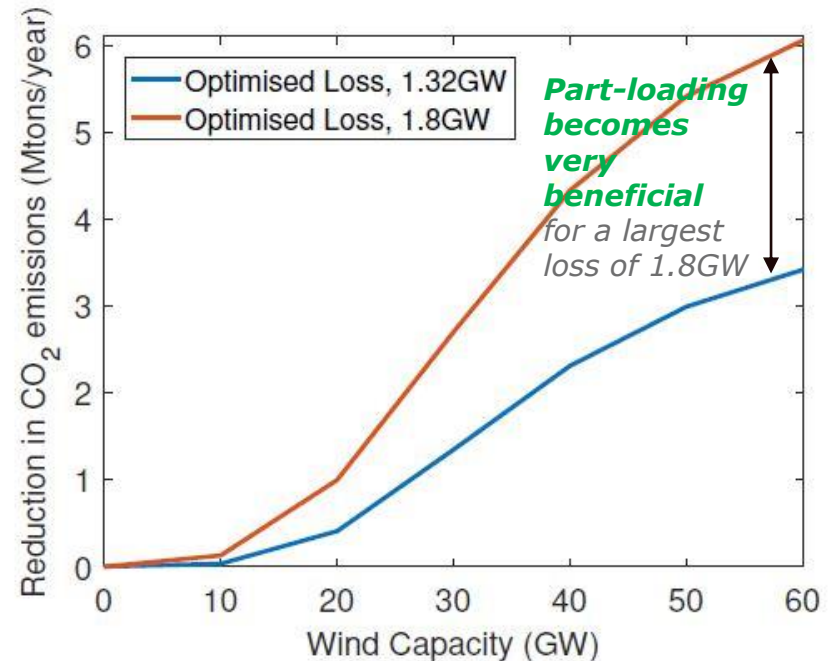
- Low-wind conditions: nuclear at full output
- High-wind conditions: nuclear part-loaded to reduce the largest loss

**Part-loading large nuclear plants can reduce overall carbon emissions!** More info [here](#)

Current largest nuclear in Great Britain: **1.32GW**

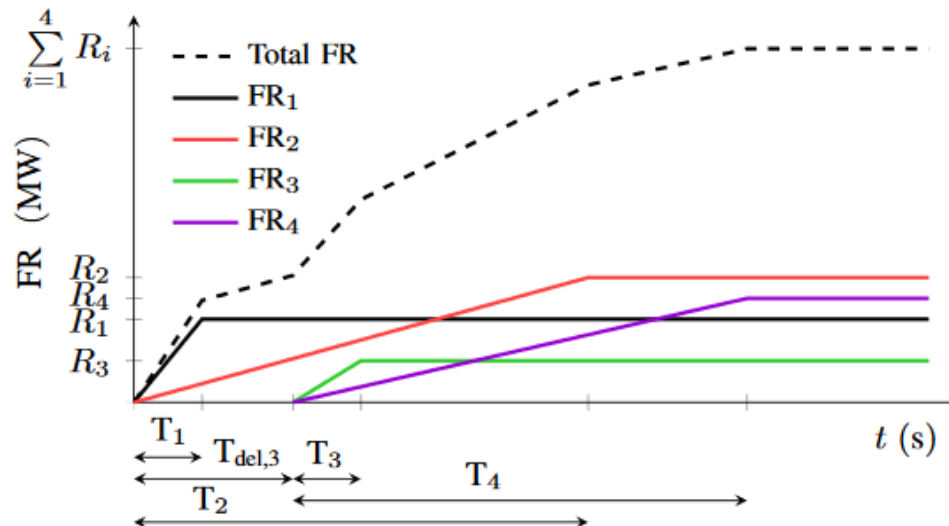


Planned largest nuclear in Great Britain: **1.8GW**



# Optimal portfolio of multi-speed frequency response

We have developed an optimisation framework that allows to consider any combination of different frequency-response speeds and activation delays:



This formulation allows to **fully extract the value of the different assets** in a power system, **putting in place the right incentives** for those assets to provide the fastest frequency response possible.

More info [here](#)

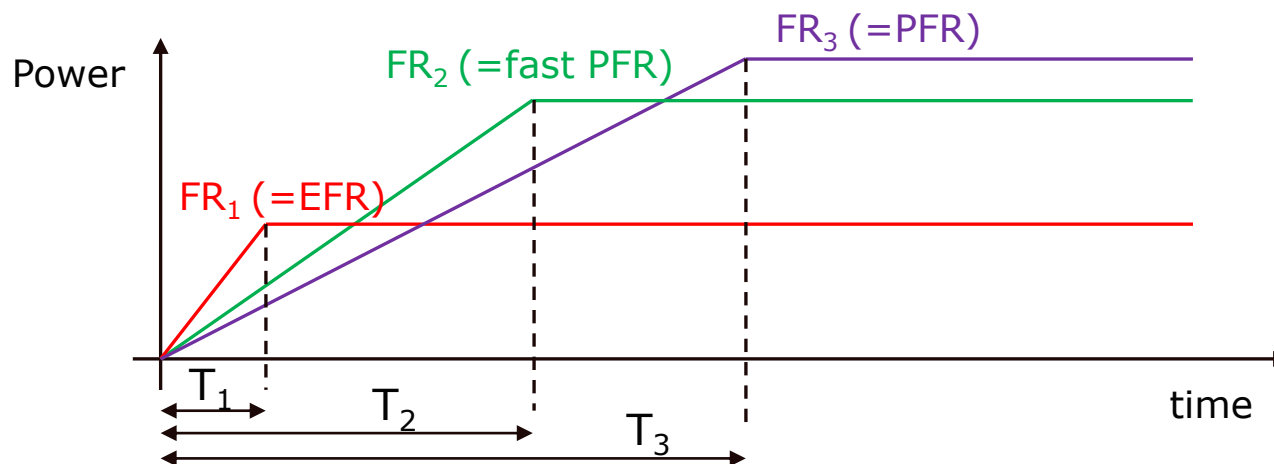


# Value of recognising different response speeds

**Beyond the EFR-PFR duo:** *is there value in creating new FR services, that are faster than PFR, but slower than EFR?*

We have shown that **there is value in ‘fast PFR’**

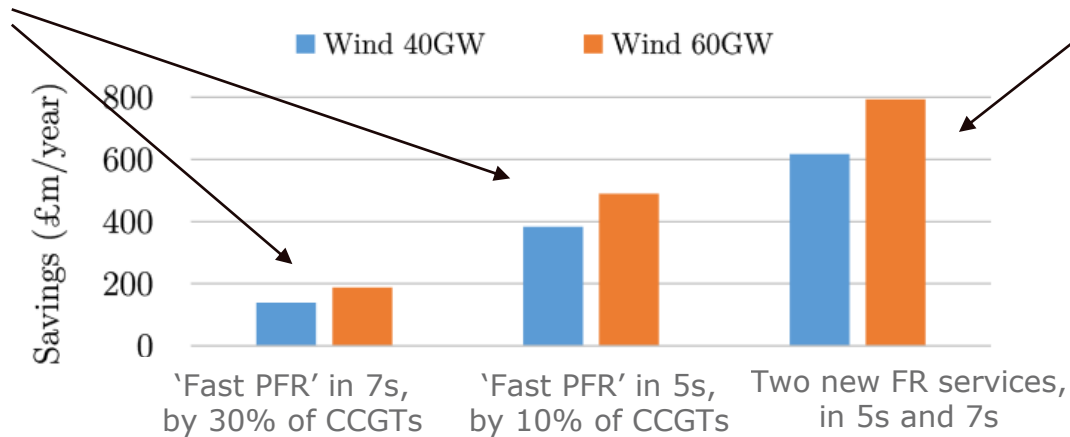
- But it is important to understand the capabilities of the system assets before defining new services: new services increase market complexity and in some cases do not bring great benefits. More info [here](#)



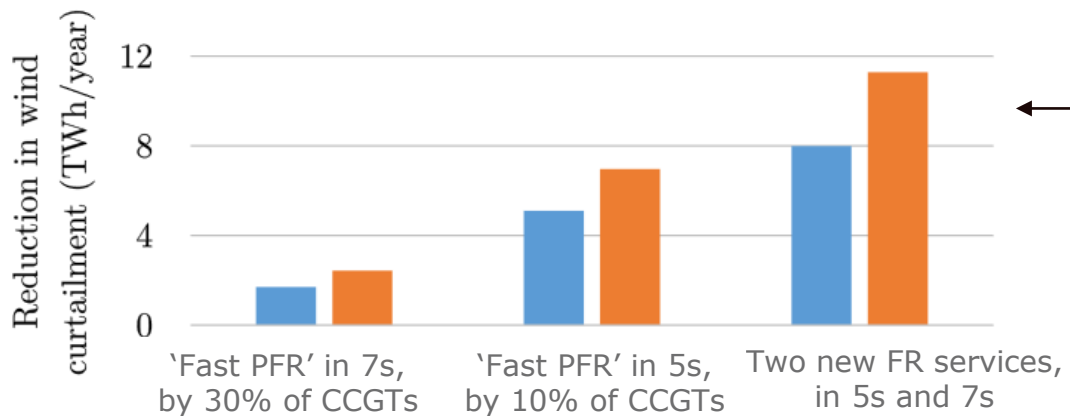
# Value of recognising different response speeds

Benefits compared to simply considering EFR+PFR in Great Britain:

Important to analyse the system thoroughly before defining a new service: 10% of CCGTs providing FR in 5s achieve higher savings than 30% providing FR in 7s



Defining new FR services can further increase savings, although market complexity increases



Faster FR services imply a lower overall volume of FR needed, therefore less thermal plants are needed online and more wind can be accommodated

More info [here](#)

# Marginal-pricing mechanism for frequency services

Taking advantage of a convex Second-Order Cone formulation we developed, we propose a pricing scheme using **duality theory**:

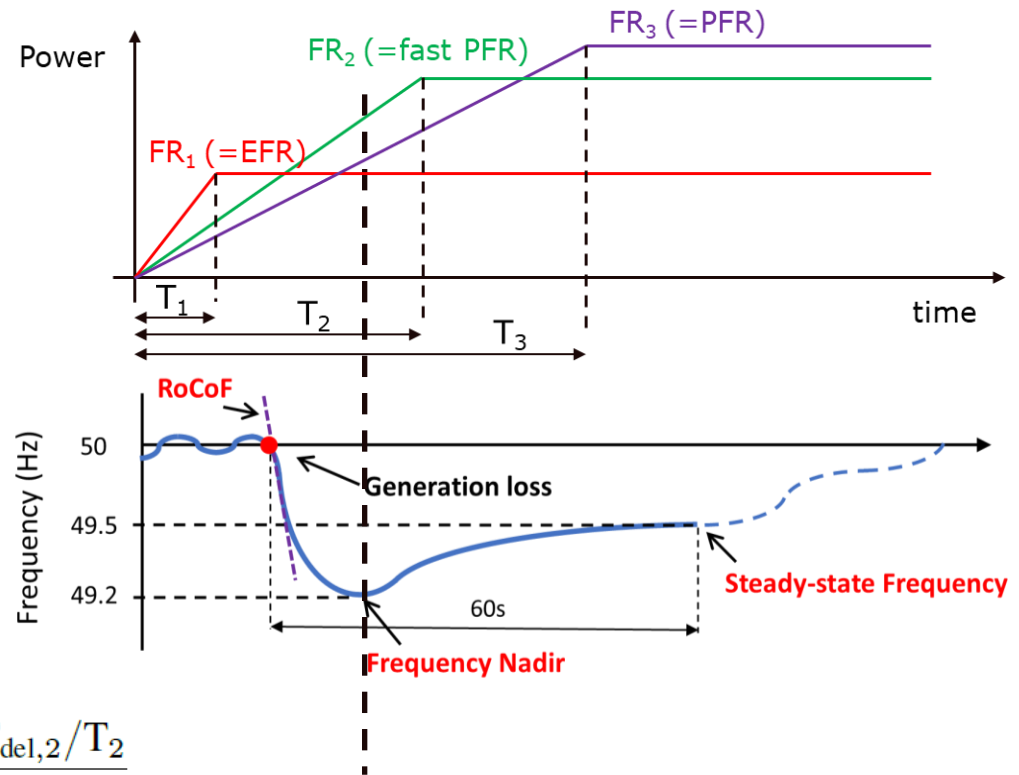
More info [here](#)

Price for fast FR services:

$$\frac{\lambda_2}{\sqrt{\Delta f_{\max}}} - (\mu - \lambda_1) \frac{T_1 + T_{\text{del},1}}{4\Delta f_{\max}}$$

Price for slow FR services:

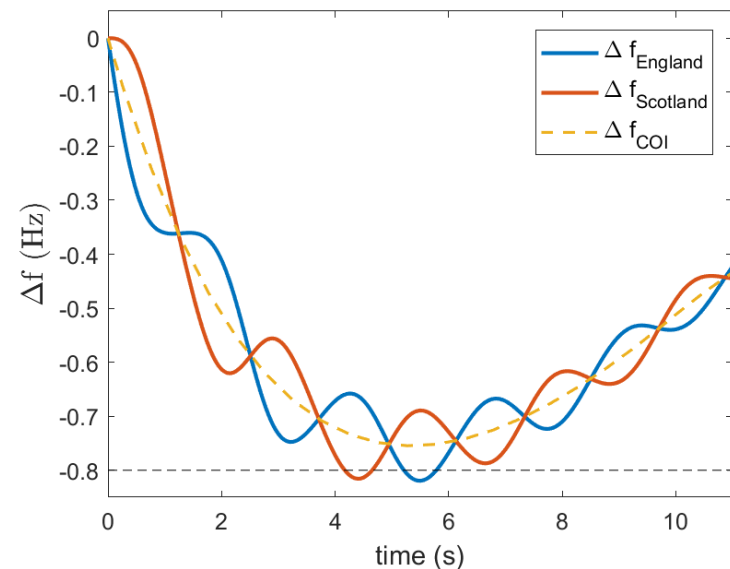
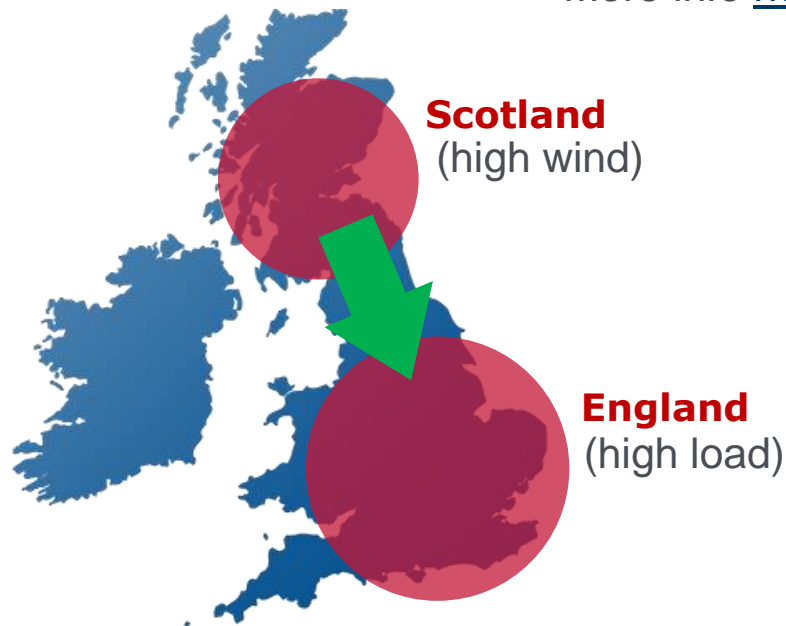
$$(\mu + \lambda_1) \frac{1}{T_2} + (\mu - \lambda_1) \frac{T_{\text{del},2}^2/T_2}{4\Delta f_{\max}} - \lambda_2 \frac{T_{\text{del},2}/T_2}{\sqrt{\Delta f_{\max}}}$$



# Conditions for regional frequency stability

- **Inter-area frequency oscillations** around the Centre Of Inertia (COI) appear when **inertia is not evenly distributed in the grid** (e.g. high wind capacity in Scotland but most of the electric demand located in England).
- **Ignoring inter-area oscillations could be dangerous:** higher RoCoFs and lower frequency nadirs than the COI could lead to unexpected blackouts.
- We have, for the first time, **deduced stability conditions for regional frequency**, and studied their implications in the Great Britain system.

More info [here](#) and [here](#)



# Summary of contributions

## For **current power systems**:

- Allows to **optimally operate the system**, for example optimally part-loading large nuclear plants to reduce the largest possible loss. Particularly valuable for systems with high renewable penetration.
- Allows to **inform market design for energy and ancillary services**, putting in place the right incentives for providers of inertia and frequency response.

## For **potential future scenarios** of generation mix or market structure:

- Allows to **study the value of different technologies** (e.g. fast power injections from battery storage, flexibility from thermal units).
- **Where in the network to place ancillary services**, guaranteeing regional frequency stability in a cost-effective manner.